

# A Tightly-Coupled UWB/INS Integration with Forward-Backward Data Fusion

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# 1. Introduction

## Outdoor Environments

GNSS



**Onboard sensors**

**Inertial Measurement Unit (IMU)**

- 3D accelerometer
- 3D gyroscope
- 3D magnetometer



In outdoor environments, GNSS/INS has been widely used for precise positioning and navigation.

# 1. Introduction

## Indoor Environments



Intelligent mobile robots



Unmanned Aerial Vehicle

### ■ Applications

- Mapping
- Exploration
- Search and rescue
- Transportation

### ■ Requirements

- Robust and accurate positioning
- Location under any circumstance

### Existing Indoor Positioning Techniques



- ◆ Limited Positioning accuracy (several meters)
- ◆ Easily be affected

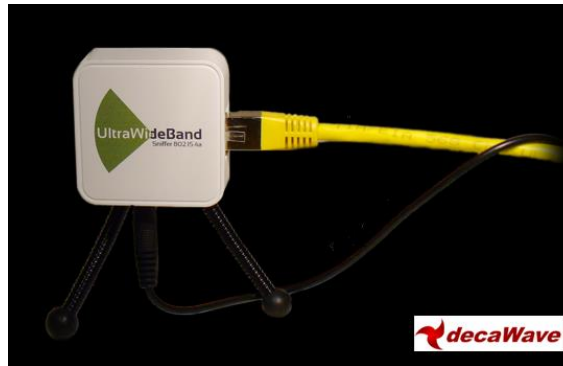
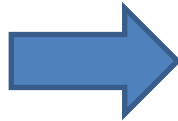
# 1. Introduction

## Challenges

Accurate position estimation will be the key.



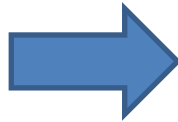
Not available in  
indoor environments



Ultra-Wideband  
(UWB) can provide  
high accuracy  
positioning results  
(cm~dm level)



High price and high weight



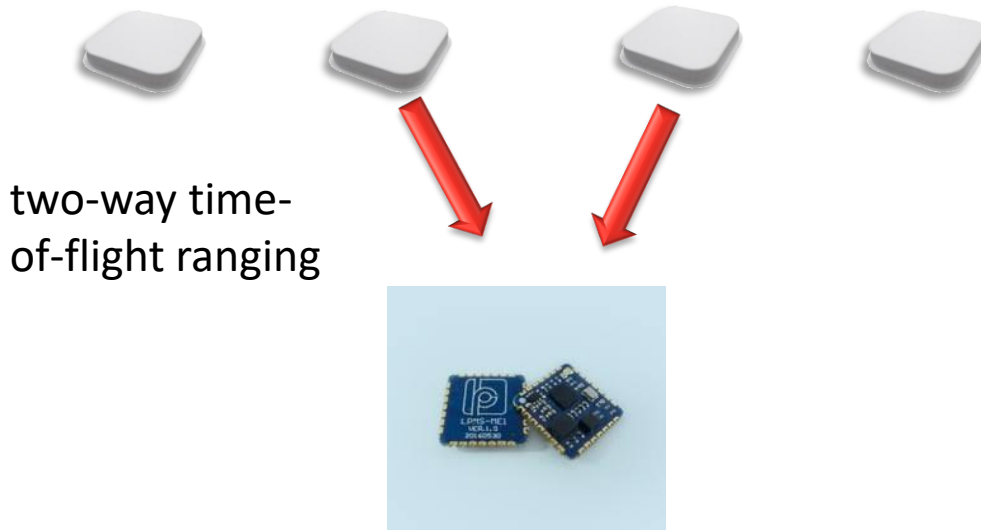
MEMS IMU: Low cost  
and Low weight



UWB/MEMS integration

# 1. Introduction

## Integration Strategies



- Loose Couple: UWB position + IMU

**Disadvantage:** at least 3 anchors are needed for UWB positioning.

- Tight Couple: UWB ranges + IMU

**Advantage:** available when UWB signal is blocked by obstacles.

**Objectives:** integrating UWB and low cost IMU to provide high accuracy positioning estimate.

## 2. Algorithm Formulation

### UWB/INS tightly coupled integration

INS mechanization

$$\dot{\mathbf{v}}^n = \mathbf{f}^n - (2\boldsymbol{\omega}_{ie}^n + \boldsymbol{\omega}_{en}^n) \times \mathbf{v}^n + \mathbf{g}_l^n$$

$$\boldsymbol{\omega}_{ie}^n = [\omega_{ie} \cos L \quad 0 \quad -\omega_{ie} \sin L]$$

$$\boldsymbol{\omega}_{en}^n = \begin{bmatrix} \frac{v_E^n}{R_N + h} & -\frac{v_N^n}{R_M + h} & -\frac{v_E^n \tan L}{R_N + h} \end{bmatrix}$$

**can be neglected for MEMS and low-dynamics applications**

$$\dot{\mathbf{C}}_b^n = \mathbf{C}_b^n \boldsymbol{\Omega}_{nb}^b = \mathbf{C}_b^n (\boldsymbol{\Omega}_{ib}^b - \boldsymbol{\Omega}_{in}^b)$$



$$\dot{\mathbf{v}}^n = \mathbf{f}^n + \mathbf{g}_l^n$$

$$\dot{\mathbf{C}}_b^n = \mathbf{C}_b^n \boldsymbol{\Omega}_{nb}^b = \mathbf{C}_b^n (\boldsymbol{\Omega}_{ib}^b)$$

**For GNSS/INS integration in the navigation frame**

**For UWB/MEMS integration in the indoor frame**



**INS error model**

$$\delta \dot{\mathbf{v}} = -\delta \boldsymbol{\psi} \times \mathbf{f} + \nabla$$

$$\delta \dot{\mathbf{r}} = \delta \mathbf{v}$$

$$\delta \dot{\boldsymbol{\psi}} = \boldsymbol{\varepsilon}$$

**Error states**

$$\begin{cases} \mathbf{x}_{Nav} = [\delta r_x, \delta r_y, \delta r_z, \delta v_x, \delta v_y, \delta v_z, \delta \psi_x, \delta \psi_y, \delta \psi_z]^T \\ \mathbf{x}_{Acc} = [\nabla_{bx}, \nabla_{by}, \nabla_{bz}, \nabla_{fx}, \nabla_{fy}, \nabla_{fz}]^T \\ \mathbf{x}_{Gyro} = [\varepsilon_{bx}, \varepsilon_{by}, \varepsilon_{bz}, \varepsilon_{fx}, \varepsilon_{fy}, \varepsilon_{fz}]^T \end{cases}$$

## 2. Algorithm Formulation

### UWB/INS tightly coupled integration

#### Measurement model

For the two-way time-of-flight ranging approach, the measurement model is composed of the range difference vector between UWB and the INS predicted value:

$$\mathbf{Z} = \begin{bmatrix} r_1^{\text{UWB}} - r_1^{\text{INS}} \\ r_2^{\text{UWB}} - r_2^{\text{INS}} \\ \vdots \\ r_i^{\text{UWB}} - r_i^{\text{INS}} \end{bmatrix}$$

where  $r_i^{\text{UWB}} = \sqrt{(x^{\text{UWB}} - x)^2 + (y^{\text{UWB}} - y)^2 + (z^{\text{UWB}} - z)^2}$

$$\mathbf{Z}_k = \mathbf{H}_k \mathbf{X}_k + \boldsymbol{\tau}$$

Extended Kalman filter (EKF) is used to fuse UWB and IMU observation, INS estimated navigation states are used to predict the UWB-observables within the EKF



## 2. Algorithm Formulation

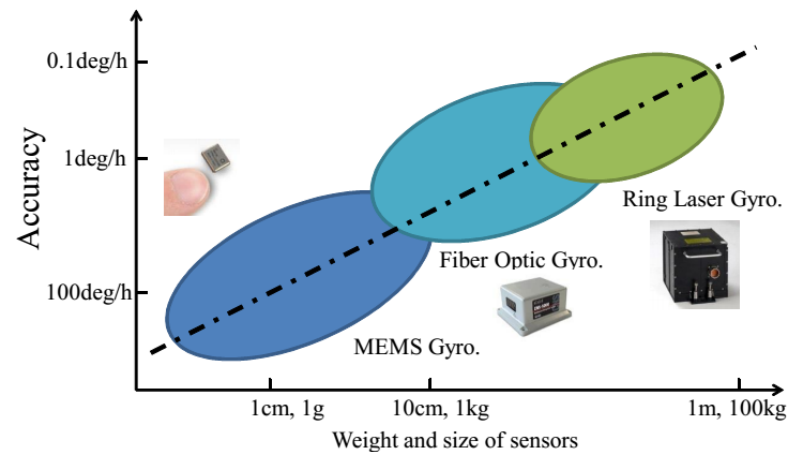
### Forward and backward integration

#### Initialization problem

**Position:** UWB positioning result ;  
**Velocity:** Static start;  
**Attitude:** pitch and roll are determined with accelerometer data;  
Heading (yaw) angle cannot be directly measured in the local navigation frame for MEMS.



**Inaccurate initial attitude requires a long period to converge.**



## 2. Algorithm Formulation

### Forward and backward integration

#### Normal INS resolution

$$\dot{C}_b^l = C_b^l (\omega_{ib}^b \times)$$

$$\dot{v}^l = C_b^l f_b + g^l$$

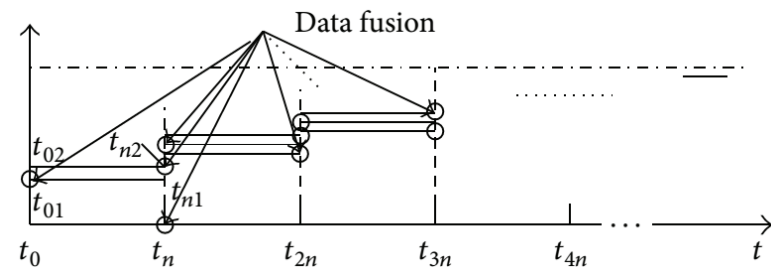
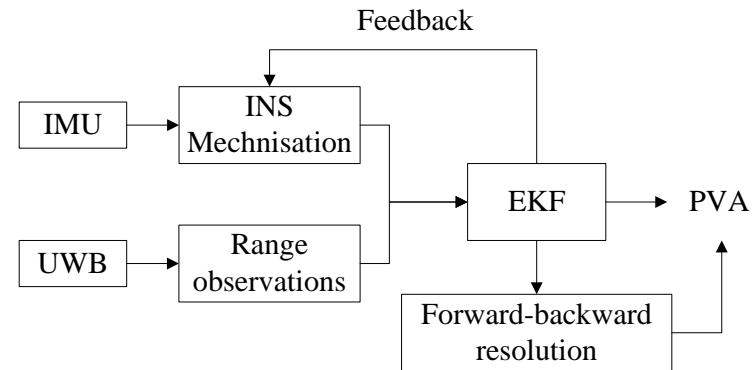
$$\dot{r}^l = v^l$$

#### Reverse INS resolution

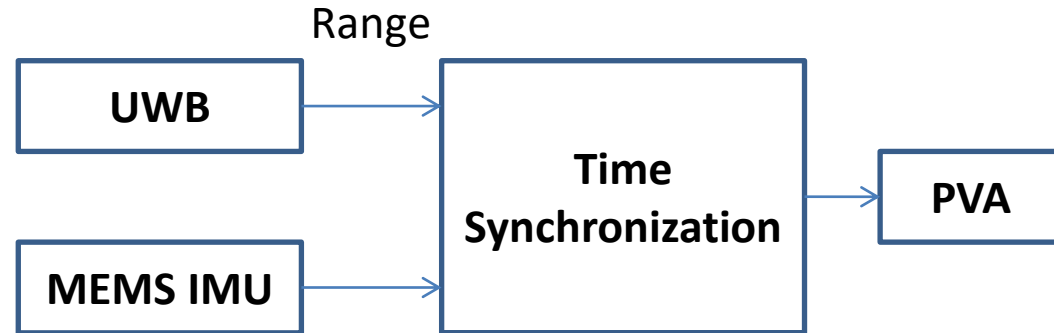
$$\dot{C}_b^l = C_b^l (-\omega_{ib}^b \times)$$

$$\dot{v}^l = -C_b^l f_b + g^l$$

$$\dot{r}^l = -v^l$$



# 3. Develop of Prototype



## Feature of Prototype

Components	5 UWB Anchors 1 UWB Tag + MEMS IMU (accelerometer & Gyro) Time Synchronization
Size & Shape	UWB 23mmx13mm



Tag



Anchor

## 4. Experiment Results

### Experimental description

**Site:** Old Main Building, UNSW

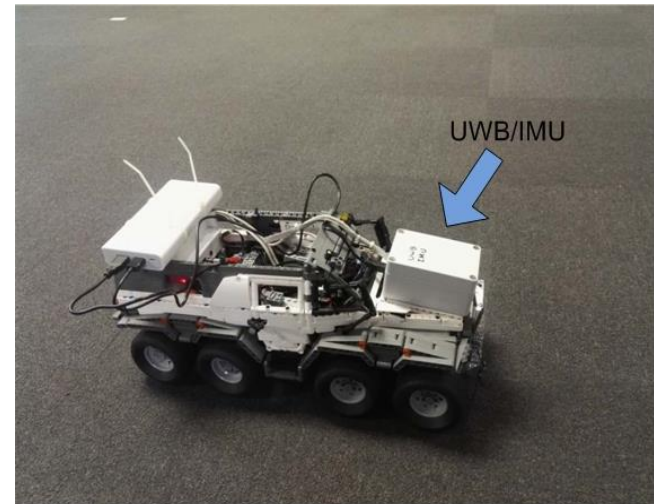
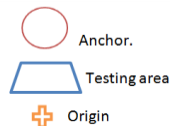
**Date:** November 2, 2017

**Equipment:** UWB (developed based on Decawave DWM1000) , 5 Hz; IMU (LPMS-ME1), 100 Hz rate.

In dynamic test, the vehicle moved along the marked trajectory as close as possible



Test environment

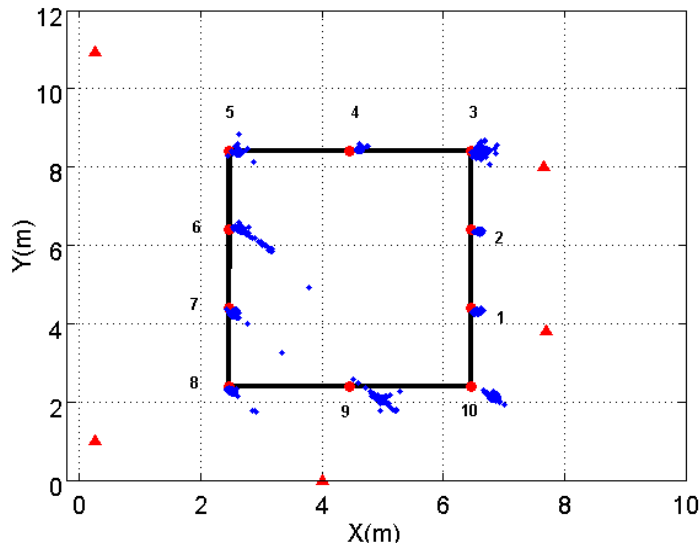


Test equipment

# 4. Experiment Results

## UWB static positioning results

- A total of **ten test points** were evenly selected in the test area;
- Positioning errors for most test points are smaller than **0.2 m** for each component;
- Large positioning errors can be observed at the test points 6, 9 and 10, which may be caused by signal blockage.



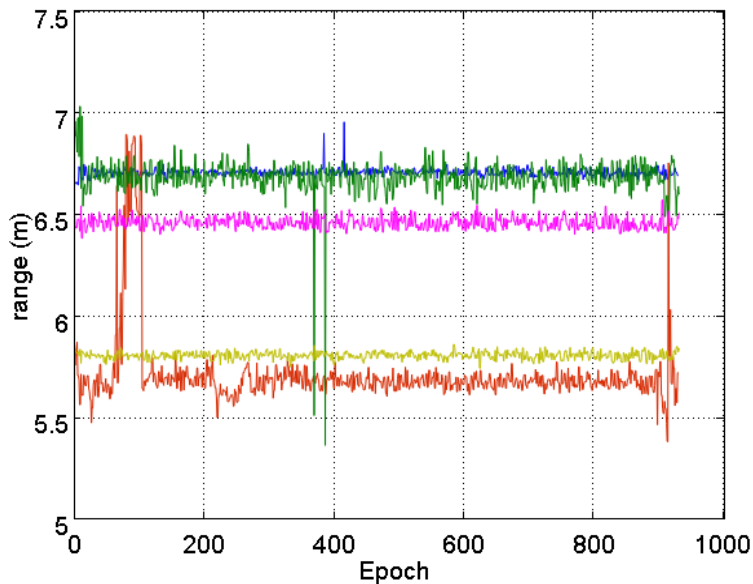
**Static positioning**

Test point	RMS (m)		MAX (m)	
	X	Y	X	Y
1	0.104	0.102	0.214	0.165
2	0.143	0.054	0.204	0.121
3	0.176	0.061	0.425	0.340
4	0.166	0.063	0.300	0.179
5	0.154	0.054	0.400	0.429
6	0.240	0.099	1.320	1.495
7	0.085	0.188	0.876	1.143
8	0.052	0.131	0.462	0.648
9	0.508	0.332	0.821	0.639
10	0.391	0.303	0.557	0.473
Mean	0.202	0.139	0.558	0.563

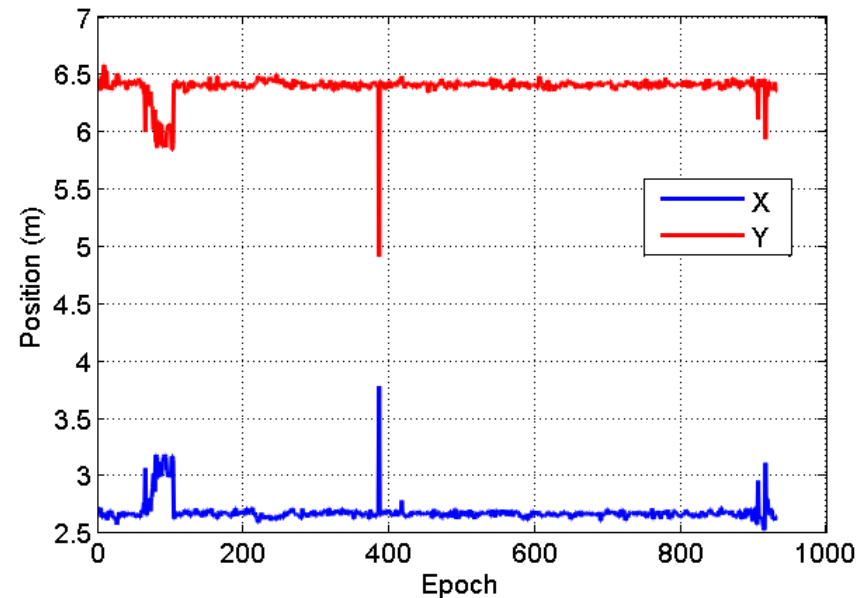
## 4. Experiment Results

### UWB static positioning results

- At test point 6, there were about 7 s (35 measurements) abnormal in the beginning period.
- The range observations from Anchor 2 (0.25,10.94) were evidently biased.



Range observations



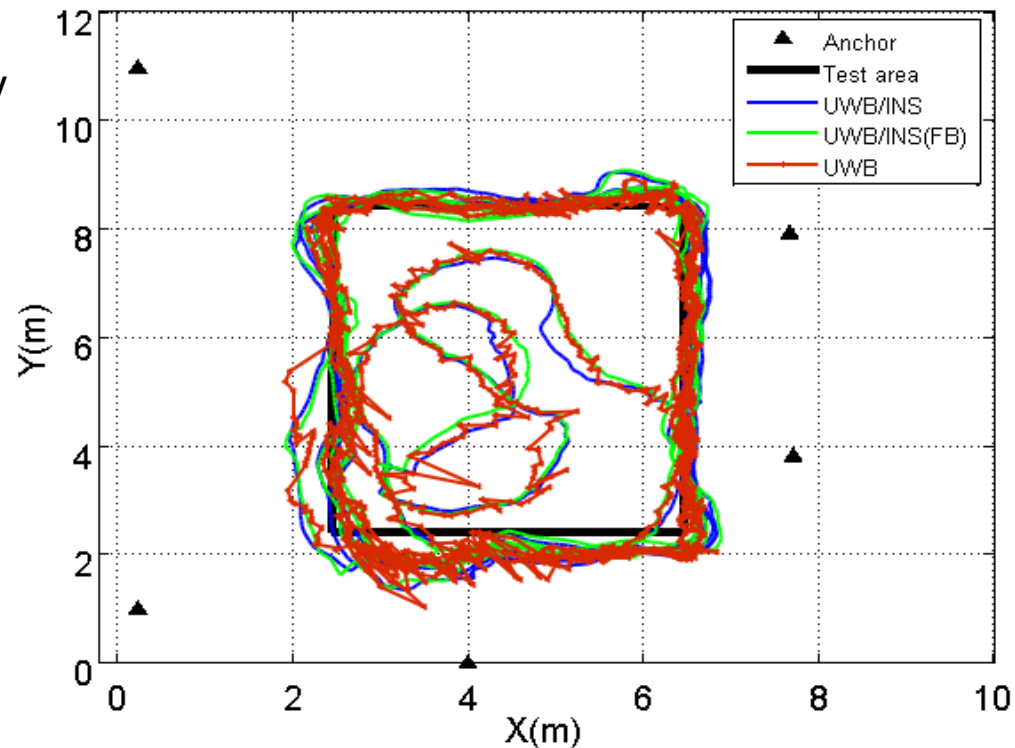
Positioning results

Test point 6

## 4. Experiment Results

### UWB/INS integration results

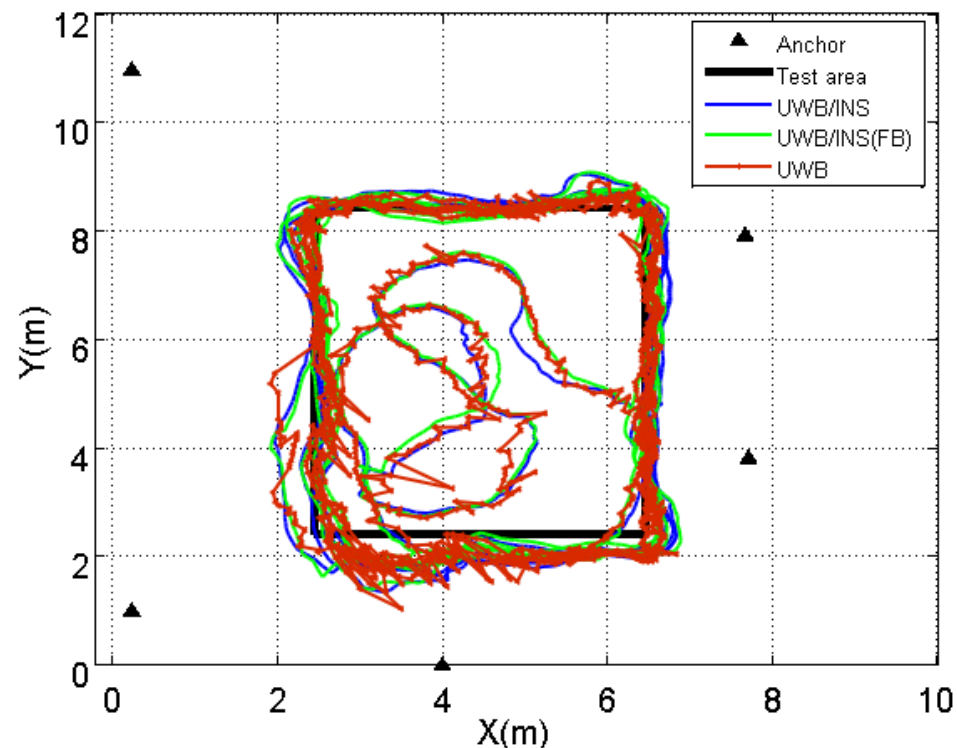
- The test vehicle pointed approximately to Y-axis during the stationary period, then conducted a “8” shape dynamic alignment;
- Three processing schemes :
  - (1) UWB positioning;
  - (2) UWB/INS tightly coupled integration;
  - (3) UWB/INS tightly coupled integration with forward-backward resolution.



## 4. Experiment Results

### UWB/INS integration results

- UWB/INS integration system can provide **superior positioning** performance compared to UWB alone;
- The integrated system can provide **more robust and smoother** positioning results;
- By applying the repeated resolution scheme, the improved positioning performance can be observed, especially when initial heading information is not accurate for the low-cost IMU.

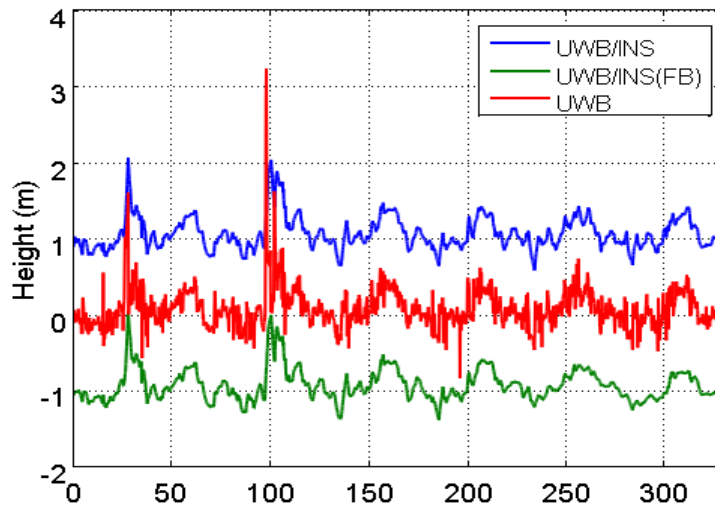




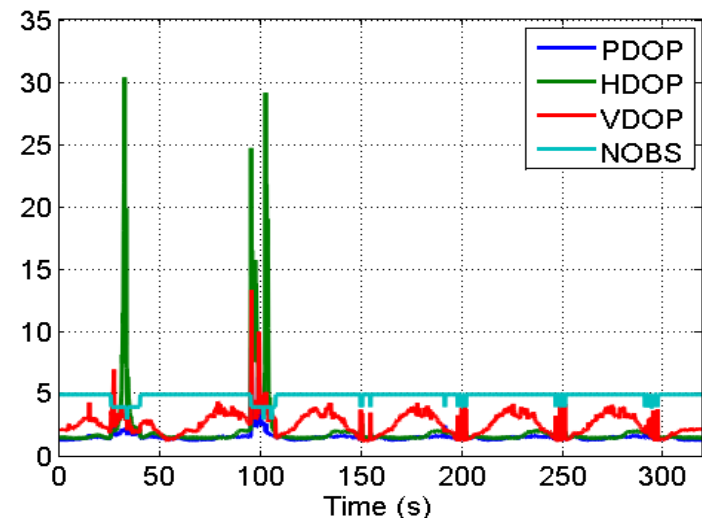
## 4. Experiment Results

### UWB/INS integration results

- The standard deviations (STD) for three schemes are 0.256 m, 0.214 m and 0.207 m.
- Max height difference are 3.148 m, 1.053 m and 0.960 m.
- The height variations are mainly affected by UWB geometric variations.



Height estimates

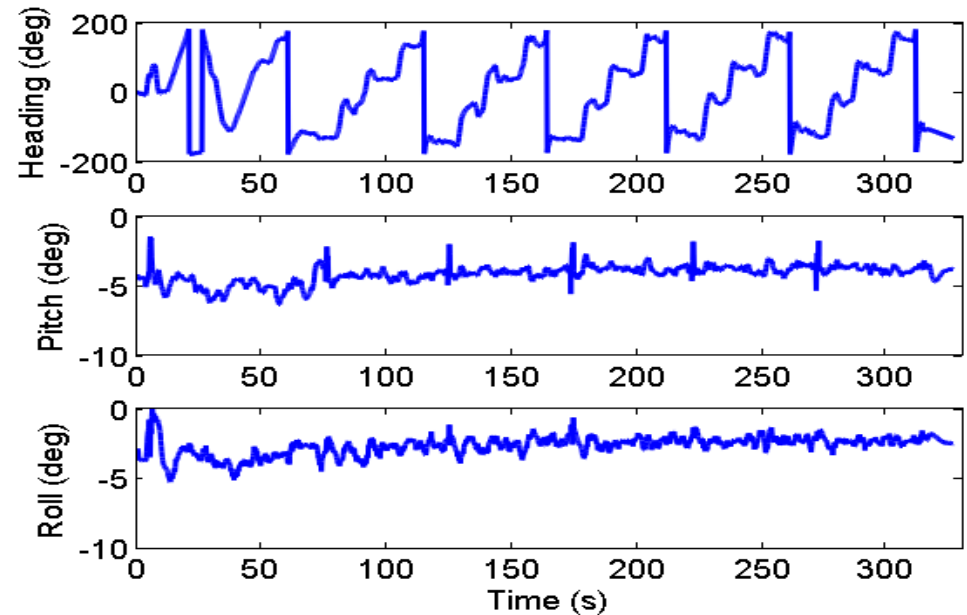


DOP value

## 4. Experiment Results

### UWB/INS integration results

- The heading angle changed periodically during the movement, while the pitch angle and roll angle remained steady without large changes.



Estimated attitude angles

## 5. Conclusions

- A tightly coupled indoor positioning system which combines UWB and INS is proposed.
- A forward-backward data fusion is proposed to improve the navigation performance.
- The static horizontal positioning errors of UWB positioning system is less than 0.2 m under the benign conditions.
- The UWB/INS integration system can provide superior positioning performance compared to UWB positioning alone.
- The added repeated resolution can improve the initial positioning performance for the low cost MEMS IMU.

**Thank you for your attention**